# Chapter 4 Airfoil and Wing/Tail Geometry Selection



# **This Section**

- Non-dimensional aerodynamic force and moment coefficients
- Wing section and planform
- Spanwise wing loading
- Winglets
- Wing location
- Tail location
- Initial tail sizing



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## Where are we now?

- Defined aircraft requirements
- Made a guess as to cruise L/D
- Made a guess as to cruise sfc
- Calculated estimate of MTOGW ( $W_{TO}$ ) and  $W_E$



# Force Ratios in Aerodynamics

#### Osborne Reynolds

#### **Reynolds Number:**

$$R_{e}(orR_{N}) = \frac{Inertia Force}{Viscous Force} = \left(\frac{\rho}{\mu}\right) VI = \frac{VI}{v}$$

#### where

 $\rho = air density$ 

- $\mu = absolute (or dynamic) viscosity$
- $\nu =$  kinematic viscosity
- V = free stream velocity
- I = representative length





Source: Kundu



Source: www.centeniallofflight.gov

https://en.wikipedia.org/wiki/Emst Mach#/media/File:Emst\_Mach 01.jpg 2023-06-29

https://commons.wikimedia.org/w/index.php?curid=5827209

**Ernst Mach** 

# Aerodynamic Forces and Moments in Plane of Symmetry





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# **Dynamic Pressure**





## Forces and Moments on a 2-D Airfoil

On atwo-dimensional section, forces and moments per unit width







#### Example of Forces on a 2-D Airfoil

- Drag is primarily due to increased shear forces
- <u>No</u> induced drag
- Note drag bucket near α
   = +/-2<sup>0</sup>



NACA 63-009 Wing





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# Lateral-Directional Forces and Moments



# Section 4.3 Wing Geometry





## Airfoil Section Geometry







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# Airfoil Sections – Infinite Choice

Ea	arly	NACA	Modern	
Wrigh	nt 1908	0012 (4 Digit)	Lissaman 7769	
Ble	eriot	2412 (4 Digit)	Ga (W)-1	
RA	NF-6	4412 (4 Digit)	Ga -0413	
Gotting	gen, 398	23012 (5 Digit)	Liebeck L1003	
Cla	urk Y	64 A010 (6 Digit)	C-5A ("Peaky")	Mostly
Mun	k M-6	65 A008 (6 Digit)	Supercritical	proprietary
			Source:Raymer	
				ADAC Aircraft Design & Consulting

# **Airfoil Section Numbering**

- NACA 4415
  - 4 = maximum camber of the mean line is 0.04c
  - 4 = position of the maximum camber is 0.4c
  - 15 = maximum thickness is 0.15c
- NACA 23012
  - 2 = maximum camber of the mean line is approximately 0.02c (design lift coefficient is 0.15 X the first digit of the series
  - 30 = position of the maximum camber is at 0.30/2 = 0.15c
  - 12 = maximum thickness is at 0.12c



# **Airfoil Section Numbering**

- NACA 65<sub>3</sub>-421
  - 6 = series designation
  - 5 = minimum pressure is at 0.5c
  - 3 = drag coefficient is near its minimum values over of a range of lift coefficients of 0.3 above and below the design lift coefficient
  - 4 = design lift coefficient is 0.4
  - 21 = maximum thickness is 0.21c



# **Typical Thickness Distribution and Twist**

Increased wing root t/c improves structural efficiency where wing bending is greatest, and provides space for main landing gear



Source: Schaufele

Wing twist reduces tendency for tip to stall first, and may also make spanwise lift distribution closer to elliptical at a given  $C_L$ 



Source: Schaufele

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# Wing Planform

- Reference wing area

   (S<sub>ref</sub>) is <u>usually</u> the area of trapezoid that approximates the wing planform, except at Boeing which includes some of yehudi
- Airbus uses modified gross wing area



# Wing Reference Area Definitions





#### Comparison between B-47 and Avro Vulcan Aerodynamic Characteristics

	Boeing B-47	Avro Vulcan	Boeing B-42
Ving Area (ft <sup>2</sup> )	1430	3446	m/th m
otal Wetted Area (ft <sup>2</sup> )	11,300	9,500	
pan (ft)	116	99	M H
Ving Loading (lb/ft <sup>2</sup> )	140	43	CAN H NO
pan Loading (lb/ft)	1750	1520	11L
spect Ratio	9.43	2.84	<u>A</u>
Dmin	0.0198	0.0069	1
$= 1/(\pi ARe)$	0.0425	0.125	Α
alue of e	0.8	0.9	(ė)
1ax L/D	17.25	17.0	Avro Vulcan
Lont	0.682	0.235	intri I
lax Cruise CL	0.48	0.167	
DminSref	28.3	23.8	
Vetted Area / Srof	7.9	2.8	

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### B-47 and Avro Vulcan Drag Polar Comparison



# Wing Planform

Given parameters: Reference (weight at block release) =  $W_o$ Wing loading =  $\frac{W}{S}$ Aspect ratio = A Taper ratio =  $\lambda$ Sweep of quarter chord =  $\Lambda_c$  $\frac{4}{4}$ 



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# Sweep of Arbitrary Fraction of Chord

General relationship between leading edge sweep and sweep at arbitrary fraction of chord:

$$\tan \Lambda_{xc} = \tan \Lambda_{LE} - 4x \frac{1-\lambda}{A(1+\lambda)}$$

where x is fraction of chord, c

$$\tan \Lambda_{\frac{c}{4}} = \tan \Lambda_{LE} - \frac{1 - \lambda}{A(1 + \lambda)}$$
  
Or  
$$\tan \Lambda_{\frac{c}{2}} = \tan \Lambda_{LE} - 2 \frac{1 - \lambda}{A(1 + \lambda)}$$

Sweep is normally defined by by  $\Lambda_{c/4},$  but for supercritical wing L/D calculations, it may be defined by  $\Lambda_{c/2}$ 





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# Mean Aerodynamic Chord

Two ways to determine MAC

- 1. Graphical
- 2. Algebraic

$$\overline{c} = \left(\frac{2}{3}\right)c_{root}\frac{1+\lambda+\lambda^2}{1+\lambda}$$
$$\overline{y} = \left(\frac{b}{6}\right)\frac{1+2\lambda}{1+\lambda}$$





# MAC of Cranked Wing

For a cranked wing planform equivalent mac is  $\overline{c} = \frac{\overline{c}_1 S_1 + \overline{c}_2 S_2}{S_1 + S_2}$ Location is defined by  $\overline{x} = \frac{x_1 S_1 + x_2 S_2}{S_1 + S_2}$  $\overline{y} = \frac{y_1 S_1 + y_2 S_2}{S_1 + S_2}$ where  $\overline{x} = x \text{ location of } \frac{c}{4} \text{ for equivalent mac}$  $\overline{y} = y \text{ location of equivalent mac}$ 



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# Strength of Free Vortex

Strength of free vortex,  $\Gamma = v' 2\pi r$ 

Circumferential component of velocity,  $v' = \frac{\Gamma}{2\pi r}$ Radial component of velocity , u' = 0





## **Distribution of Circulation**

Put spanwise location, y, in terms of  $\theta$  where  $y = -s \cos\theta$ Define spanwise distribution of circulation,  $\Gamma$ , as a Fourier series  $\Gamma = -U4 s \sum_{n=1}^{\infty} A_n \sin n\theta$ Total lift

$$L = -\int_{-s}^{s} \rho U \Gamma dy$$





# Distribution of Circulation for Minimum D<sub>i</sub>

All terms in Fourier series contribute to drag so for minimum induced drag  $A_2 = A_3 = A_4 = ... = 0$  $\Gamma = -4 \text{ Us } A_1 \sin \theta$  $\cos \theta = \frac{y}{s}$  so  $\sin \theta = \sqrt{1 - \frac{y^2}{s^2}}$  $\Gamma = -4 \text{ Us } A_1 \sqrt{1 - \frac{y^2}{s^2}}$  $\left(\frac{\Gamma}{-4 \text{ Us } A_1}\right)^2 + \left(\frac{y}{s}\right)^2 = 1$ 

i.e. spanwise elliptic distribution of  $\Gamma$ 



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# Planform with Minimum Induced Drag



Elliptical planform has minimum induced drag at all values of C<sub>L</sub>

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# Trends in Wing Aspect Ratio and Taper Ratio

Aircraft Type	Aspect Ratio (AR)	Taper Ratio (λ)
Personal/Utility	5.0 - 8.0	0.6 - 1.0
Commuter Airliner	9.0 - 12.0	0.5 - 1.0
Regional Turboprop	11.0 - 12.8	0.4 - 0.6
Business Jet	5.0 - 8.8	0.4 - 0.6
Jet Transport	7.0 – 9.5	0.2 - 0.4
Military Fighter/Attack	2.4 - 5.0	0.2 - 0.5

Source: Schaufele

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## Schrenk's Approximation for Rectangular Planform

- Wing <u>section</u> aerodynamic load = (lift per unit span)/chord
- For an unswept, untwisted wing, lift distribution is represented by line midway between planform chord distribution and ellipse of equal area



#### **Downwash Effect is Accentuated**

 Untapered, untwisted wing can have close to elliptical (minimum drag due to lift) lift distribution



Source: Raymer

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### If Wing is Swept Forward



• Low-cost bomber concept

Source: Raymer

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### Schrenk's Rule for Delta Planform

- Likelihood of
   asymmetric stall
- Increased transonic drag





### **Development of Avro Vulcan Planform**



## C<sub>I</sub> as function of span for typical transport wing

- Ensure that wing stalls near root first
- Leave outboard margin for spanwise boundary layer migration


## SR-71 Leading Edge Washout



Source: commons.wikipedia.org



# Flow Over Wing At Increasing Mach Number



## Flow within Supersonic Region

 System of expansion and compression waves exist within supersonic flow region



Source: Obert

Source: Schaufele

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# Swept wing thought experiment



Imagine an infinitely long wing moving at velocity v perpendicular to the wind tunnel flow, and that you are a bacterium sitting on the wing. Your apparent wind is V<sub>∞</sub>

Source:McCormick

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### 1935 Volta Conference

Dr. Adolf Busemann suggested swept wings for supersonic flight
Arturo Crocco sketched out design of supersonic airplane on back of menu at dinner



By NASA, Public Domain, https://commons.wikimedia.org/w/index.php?curid=384224

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# Effects of Sweep on $C_{D_0}$

• Sweep decreases and delays drag rise • At M=2+, C<sub>Do</sub> increases with sweep



### Wing Design Charts for Transonic Cruise Aircraft

- Average t/c is defined as <u>Wing frontal area (untwisted)</u> Wing planform area
- Chart applies to supercritical airfoil sections with a given level of technology
- For given wing characteristics (sweep and average t/c) and cruise C<sub>L</sub>, M<sub>DD</sub> can be estimated
- Charts available for  $\Lambda = 0$ , 15, 25, 35 deg.



ource. Schaulele

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## Wing Design Charts for Transonic Cruise Aircraft

- For a given M<sub>DD</sub> and cruise C<sub>L</sub>, tradeoff exists between wing sweep (Λ) and t/c
- Evaluate tradeoff using detailed aircraft synthesis and sizing program



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### Drag Divergence Mach Number (M<sub>DD</sub>)

Definitions of Drag Divergence Mach Number Boeing :

 $M_{DD}$  occurs when  $C_D(@M_{DD}) - C_D(@M_{CRIT}) = 0.0020$ i.e. when the airplane is flying 20 counts into the drag rise.

Douglas :

Douglas definition more generally accepted

<u>Very</u> approximate

 $M_{DD}$  occurs when  $\frac{dC_{D}}{dM} = 0.10$ i.e. when the gradient of the drag rise curve is 0.10

Raymersuggests  $M_{DD(Douglas)} \approx M_{DD(Boeing)} + 0.06$ 

(Note that one drag count is defined as  $\Delta C_{D} = 0.0001$ )

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# Tool for Comparing Wing Technology



Airbus wing design not surpassed until 737NG series in 1997

Source: Obert



# More Generalized Analysis Using Extended Korn Equation

$$\left(\mathsf{M}_{\mathsf{dd}}\right)_{\mathsf{Douglas}} = \frac{\kappa_{\mathsf{a}}}{\cos\left(\Lambda_{\frac{\mathsf{c}}{2}}\right)} - \frac{\frac{\mathsf{l}}{\mathsf{c}}}{\cos^{2}\left(\Lambda_{\frac{\mathsf{c}}{2}}\right)} - \frac{\mathsf{C}_{\mathsf{l}}}{\cos^{3}\left(\Lambda_{\frac{\mathsf{c}}{2}}\right)}$$

where

 $M_{dd}$  = section drag divergence Mach number, where  $\frac{dC_{d}}{dM} = 0.1$ 

$$\kappa_a = \text{technology factor}$$

 $\Lambda_{\underline{c}} = sweep of mid-chord$ 

 $\frac{t}{c} = section$  thickness to chord ratio

C<sub>1</sub> = **section** lift coefficient

Wing planform may divided into series of panels and wave drag contributions summed

Source:: Gundlach Section 5.8.5



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### Typical Values of $\kappa_a$ in Korn Equation

Wing or Aircraft	к <sub>а</sub>
NACA 6-series section*	0.87
Generic supercritical*	0.95

\* Grasmeyer



# LE Sweep and t/c Trend Lines





Source: Raymer



### Winglet Design



Source: Aviation Week advertisement

#### • Take advantage of crossflows near wingtips due to tip vortices



# Winglet Design



https://aviation.stackexchange.com/questions/55992/why-do-i-see-moisture-coming-from-the-middle-of-the-wing-as-well-as-wingtip-vort

Winglets appear to weaken tip vortices



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# Winglet Action



• Similar to that of sailing boat sailing into the wind.





### Plan View of Winglet

- Exaggerated inflow angle on upper surface
- Inflow angle is a function of wing C<sub>L</sub>
- If winglet incidence is incorrect, then thrust may become drag



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### Winglet Installation on Existing Wing Design

- Smooth transition to minimize mutual interference
- Installation of B.757 winglet for UAL shown

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### Winglet Installation on 737 MAX



Source: www.boeing.com

Integrated wingtip/winglet design can use smaller radius fillet

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# High Wing

- Advantages
  - Continuous wing upper surface (high L/D)
  - Clean propeller nacelle
  - Short airstairs
  - Easy baggage loading





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# High Wing

#### • Disadvantages

- For jets, MLG on fuselage (more drag, narrow track)
- For jets, landing wing inertia loads carried through wing root
- Main spar passes through cabin
- Pax view impaired



Source: John Wright

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# Low Wing

#### Advantages

- Wing box under cabin floor
- Easier landing gear installation (esp. for large transport aircraft)
- Good visibility for pax





# Low Wing

#### • Disadvantages

- Difficult to install high BPR engines under wing
- Interference drag between wing and fuselage
- Difficult to install airstairs



https://www.ndtv.com/world-news/boeing-says-its-open-to-changing-the-name-of-grounded-737-max-jet-2054867



# F-22





# F-117

- Shield inlet and nozzle from ground-based missiles
- Minimize reflections from ground radar





## F-35A

 Requirements for air superiority not as stringent as for F-22



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# Box Wing

- Advantages
  - Higher span efficiency
- Disadvantages
  - Difficult to integrate landing gear
  - Difficult to access passenger cabin
  - Insufficient wing volume for fuel



Lockheed Martin Box Wing concept



# Joined Wing

- Advantages
  - Lighter structure
  - Good locations for multiple antennae
- Disadvantages
  - Must locate MLG in fuselage
  - Doesn't work well with long fuselage
  - Complex aerodynamics
  - Interference at wing join



A Boeing joined-wing, SensorCraft, undergoes testing at NASA Langley's 16 X 16-ft. wind tunnel in 2010.

Source: Aviation Week

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# **Combined Box Wing/Joined Wing**

- Advantages
  - Reduced interference at join
  - Good locations for multiple antennae
- Disadvantages
  - Need strong joint at bend of rear
  - Complex aerodynamics



The model in the foreground was prominently displayed at China's Zhuhai air show and provides a good view of the new UAV's unique planform.

Source: Aviation Week



# Truss-Braced Wing (TBW)



Source: Aviation Week

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- 777-sized airplane
- High AR reduces induced drag
- Narrow chord promotes
   laminar flow
- Fuel burn reduction of 39% claimed

- Induced drag is only about 40% of total drag at high subsonic cruise
- Laminar flow is not a sure thing
- Must contend with strut interference drag

## **Canard Configuration**

#### Advantages

- Both surfaces are lifting
- Benign stalling characteristics
- Canard can be used as active control surface



Rutan Vari-Eze

Source: Raymer



BAeTyphoon

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# **Canard Configuration**

- Disadvantages
  - CG (and fuel tanks) forward of the wing
  - No wing root bending relief from fuel
  - More difficult to integrate landing gear
  - Larger nose-down pitching moment when flaps deployed
  - Non-uniform flow over wing
  - Shorter vertical stabilizer moment arm
  - May obscure pilot's view (see previous slide)



Beech Starship

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### **3-surface Configuration**

 Airbus concept uses horizontal stabilizer to shield noise from unducted fan



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# **3-surface** Configuration

- Canard surface provides trim, aft surface provides control
- Advantages
  - Theoretical optimum spanwise lift distribution
  - Can put wing spar through middle of fuselage
- Disadvantages
  - More control surfaces implies greater maintenance
  - More difficult to integrate landing gear
  - Non-uniform flow over wing



Piaggio Avanti



Airbus UDF concept



## Forward-swept Wing

- Advantages
  - Fast roll response
  - Avoids tip stall
  - In bizjet, can put wing spar through middle of fuselage
- Disadvantages
  - Root stall may cause pitchup
  - Needs structural tailoring to avoid divergence
  - Reduced efficiency of swept flaps



Source: Raymer



Source: www.hansajet.de HFB-320 Hansa Jet





# Blended Wing-Body

- Disadvantages (cont'd)
  - More difficult cargo loading and aircraft servicing
  - More difficult engine access
  - Excessive cabin motion when maneuvering
  - Difficult longitudinal trim (especially when using high-lift devices)
  - Non-uniform flow into engine nacelles at high  $\alpha$


### Blended Wing-Body

- Advantages
  - Higher L/D
  - Noise shielding of jet engines
- Disadvantages
  - Increased weight of noncylindrical passenger cabin
  - Difficult passenger access/egress





# Section 4.5 Tail Geometry and Arrangement



## **Tail Layout Options**



- Benefits of Inverted V or Y-tail
  - Offers appropriate stability and control
  - Clean air (not disturbed by wing or fuselage) over high range of α
  - Lightweight
  - Protects pusher propeller

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• Can get inside hangar

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## Preferred HT Location



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# McDonnell Douglas F-3H





#### McDonnell Douglas F-4E



Avoids blanketing of tail at high  $\alpha$ 

Outer wing panel dihedral adds roll stability lost when setting anhedral on horizontal tail

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Source: commons.Wikipedia.com

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# Tail Geometry for Spin Recovery



#### **Twin Ventral Fins**



"Learjet45-gama" by MilborneOne at English Wikipedia

- Nose-down pitching moment at stall
- Increased directional stability at high α

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#### Inward Canted Vertical Fins



Source: urbanghostsmedia.com

Lockheed Have Blue

- Gives partial shading of hot exhaust from heat-seeking missiles
- Eliminates corner reflector from vertical stabilizer



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# **Preliminary Tail Sizing**

An alternative method of graphically calculating the location of the MAC

1. Extend the tip chord forward and aft by the length of the wing root 2. Extend the root chord forward and aft by the length of the tip 3. Draw diagonals from the ends of the extended lines 4. Their intersection is the <u>mid-chord</u> of the MAC



Source: Jenkinson

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### **Tail Volume Coefficients**



Vertical tail quarter mean aerodynamic chord position

Source: Jenkinson

#### Horizontal and Vertical Tail Volume Coefficients

Aircraft Category	V <sub>HT</sub>	V <sub>vT</sub>
Sailplane	0.50	0.02
Homebuilt	0.50	0.04
GA – single engine	0.70	0.04
GA – twin engine	0.80	0.07
Agricultural	0.50	0.04
Twin turboprop	0.90	0.08
Flying boat	0.70	0.06
Jet trainer	0.70	0.06
Jet fighter	0.40	0.07
Military cargo/bomber	1.00	0.08
Jet transport	1.00	0.09

Use these values for initial estimates. Tail areas will be determined by stability and control analysis

Source: Raymer

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#### Where are we now?

- Have rough estimate of TOGW
- Have preliminary layout of airplane geometry
- Estimate of (T/W)<sub>ref</sub> and (W/S)<sub>ref</sub>
- Hence thrust required and wing area
- Select AR, t/c,  $\Lambda$ ,  $\lambda$
- Estimate tail volumes



# Airfoil and Wing/Tail Geometry Selection

The End

